A Modified Supertwisting Sliding Mode MPPT for PV system

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Abstract: This paper focuses on the control of photovoltaic systems using sliding mode control (SMC). Considering the oscillation problems that appear in the classical sliding mode control, which can affect the output power generated by the photovoltaic panel, many studies have proposed a super twisting sliding mode control (STSMC) to minimize the chattering phenomena associated with classical SMC. However, to further reduce oscillations, this work proposes a modified super twisting SMC that incorporates a fractional integrator to increase its flexibility and performance. To demonstrate the enhancements achieved with the proposed controller, a comparative simulation is implemented using Matlab/Simulink software. The results obtained highlight a significant reduction in oscillations, and clearly indicate the superiority of the modified STSMC controller over its classical counterpart.

Keywords: Photovoltaic systems, Maximum power point tracking, Sliding mode control, Modified super twisting SMC, Chattering phenomena, DC-DC boost converter

1. INTRODUCTION
Nowadays, the world’s demand for energy is substantial and continuously increasing. While traditional sources offer significant energy production, they come with notable drawbacks, including environmental pollution and the accelerated depletion of these traditional energy sources [1]. Consequently, most countries are showing interest in renewable energy sources such as wind, biomass, hydropower, photovoltaic, green hydrogen, and geothermal, along with their respective technologies, to meet their power requirements with less pollution [2], [3]. Among the most important of these sources is solar energy, which includes photovoltaic panels and solar mirror reflectors. The photovoltaic system, in particular, is widely used due to its ease of implementation, low construction costs, and minimal maintenance requirements compared to other systems [4]. To extract the maximum power from a PV panel, numerous strategies have been developed in the literature to track the maximum power point. These include traditional techniques such as perturb and observe (P&O), incremental conductance (INC), and proportional-integral (PI) control [5], [6], as well as techniques based on artificial intelligence, such as fuzzy logic control (FLC), artificial neural networks (ANN) [7], [8], particle swarm optimization (PSO), and grey wolf optimizer (GWO) [9], [10]. Additionally, advanced control methods like sliding mode control [13], super-twisting sliding mode control [17], and backstepping control [20] have also been investigated. In the paper [21] Fractional-order proportional-integral super twisting SMC is developed to enhance the wind energy system equipped with DFIG. The third order SMC is applied to PV system to improve the power quality and reduce the steady oscillations in [22].

In [11] a new sliding mode controller was designed to extract the MPP generated by the PV panel under variable weather conditions. The author used a boost converter and implemented the method in real-time to demonstrate its performance and validity. In [12] sliding mode control was applied to achieve the MPP for a standalone PV system, and to supply the load with high efficiency and accuracy. The method controlled both the boost converter and the inverter. The simulation results were compared with the traditional incremental conductance method, demonstrating that the sliding mode control method is more efficient than the INC. In [13], an adaptive backstepping sliding mode controller is proposed with the objective to regulate both the DC link voltage and the current injected...
on the AC side in the photovoltaic grid-connected system with battery energy storage system (BESS). The simulation results obtained are compared with Proportional Integral (PI) and CBC methods. The novel technique displayed superior performance compared to the other two approaches. In [14], a hybrid backstepping super twisting sliding mode control is designed to enhance the operation of the MPPT based on a super twisting-SMC. The method also incorporates a differential flatness approach (DFA) to estimate the system state variables. This strategy is applied in a standalone PV system using a cascaded non-inverting buck-boost converter, which supplies a DC charge. The developed technique is more efficient, robust, has less chattering, and has a higher performance than other techniques such as backstepping, SMC, and PID. In paper [15], a super twisting SMC method is proposed to control the inverter of a three-phase grid-connected PV system. This approach aims to optimize the current and voltage injected into the grid, thereby improving power quality and minimizing the total harmonic distortion (THD) effect under normal conditions or in the presence of perturbations. In [16], the author applies the super twisting SMC to extract the maximum power point in a PV system under variable weather conditions. Cuckoo search (CS) optimization is also employed to enhance the operation of the super twisting SMC and accurately achieve the MPP with fewer oscillations and a faster response time.

In this paper, a modified super twisting SMC is applied to track the MPP under varying weather conditions using a boost converter. The novel aspect of this controller is the incorporation of a fractional integrator into the super twisting SMC. This increases the number of variables to be tuned, providing greater flexibility and enhancing the capability of the proposed controller.

2. PHOTOVOLTAIC PANEL MODEL

Green energy production has recently become a significant global challenge, with photovoltaic systems emerging as one of the most important and attractive sources. A photovoltaic panel produces energy by directly converting sunlight into direct current (DC). Various panel types exist in the market, such as monocrystalline, polycrystalline, and thin-film, among others. These types vary in terms of material, cost, efficiency, and lifespan, etc. The equivalent circuit of a photovoltaic cell is presented in Fig. 1.

The photovoltaic cell current equation is provided as follows:

$$I_{ph} = I_d + I_o + I_{pv} \quad (1)$$

The diode current $I_d$ is given by:

$$I_d = I_a \left[ \exp \left( \frac{V_{pv} + R_s I_{pv}}{V_{oc} a} \right) - 1 \right] \quad (2)$$

The saturation current $I_o$ relation is presented as follows:

$$I_o = I_{as} \left( \frac{T}{T_r} \right)^3 \exp \left[ \frac{qE}{ak} \left( \frac{1}{T} - \frac{1}{T_r} \right) \right] \quad (3)$$

The expression for the thermal voltage of the cell is given by:

$$V_{th} = \frac{KT}{q} \quad (4)$$

where: $R_s$ and $R_p$ is the series and the parallel resistance respectively. $K=1.3805e-23 \; j/k$ is the Boltzmann constant. $T_{ref}=25^\circ c$ is the reference temperature (standard conditions), $T$ is the cell temperature. $q=1.6e-19 \; C$ is the charge of electrons. $E$ is the band gap energy depends on semiconductor material used in photovoltaic cells. $a=1.3$ is the diode ideality factor.

The reverse saturation current equation is given by:

$$I_n = \frac{I_{as}}{\exp \left[ \frac{qV_{nc}}{N, k a T} \right] - 1} \quad (5)$$

The current passes in the resistance $R_p$ is calculated as follows:

$$I_p = \frac{V_{pv} + R_s I_{pv}}{R_p} \quad (6)$$

From the Eq. (1), we determine the current $I_{pv}$ produced by PV cell:

$$I_{pv} = I_{ph} - I_d - I_p \quad (7)$$
By substitution Eq. (2) and Eq. (6) into Eq. (7), the resulting equation is:

\[ I_{pv} = I_{dc} - I_{f} \left( \frac{V_{pv} + R_{f} I_{pv}}{V_{dc}} \right) \left( \frac{V_{pv} + R_{f} I_{dc}}{R_{f}} \right) \]  

(8)

The photocurrent \( I_{dc} \) relation is expressed by:

\[ I_{dc} = \left( I_{sc} + K_{i}(T - T_{r}) \right) \frac{G}{G_{r}} \]  

(9)

\( I_{sc} \) is the short-circuit current, \( K_{i} \) is the temperature coefficient, \( G \) (W/m²) = 1000 is the reference irradiation (standard conditions), and \( G \) (W/m²) is the irradiation in the cell surface.

3. BOOST CONVERTER MODEL

The boost converter is a necessary component for stepping up voltage and supplying a DC load. The following figure shows the structure of this converter.

![Fig. 2 Circuit of the boost converter.](image)

The mathematical model of the boost converter is presented below. There are two possible operating modes, depending on whether the IGBT is on or off.

- Switch ON: in this case, the IGBT switch is closed.

\[
\begin{align*}
\frac{dI_{pv}}{dt} &= \frac{V_{pv}}{L} \\
\frac{dV_{dc}}{dt} &= -\frac{I_{pv}}{C_{out}R} \\
\end{align*}
\]  

(10)

- Switch OFF: in this case, the IGBT switch is open.

\[
\begin{align*}
\frac{dI_{pv}}{dt} &= \frac{V_{pv} - V_{o}}{L} \\
\frac{dV_{dc}}{dt} &= \frac{I_{pv} - V_{o}}{C_{out}R} \\
\end{align*}
\]  

(11)

Finally, the dynamic model of the boost converter is given as follows:

\[
\begin{align*}
\frac{dI_{pv}}{dt} &= \frac{V_{pv} - V_{o}(1 - U)}{L} \\
\frac{dV_{dc}}{dt} &= \frac{I_{pv}(1 - U) - V_{o}}{C_{out}R} \\
\end{align*}
\]  

(12)

Where \( V_{pv} \), \( V_{o} \) are the PV voltage and output voltage respectively, and \( U \) is the duty cycle. The previous dynamic model can be used to calculate the boost converter parameters.

The duty cycle of the converter can be written as:

\[ U = \frac{V_{o} - V_{pv}}{V_{o}} \text{, with } U \in [0, 1] \]  

(13)

The inductance is determined using the equation below:

\[ L = \frac{U \times V_{pv}}{f_{sw} \times \Delta I_{L}} \]  

(14)

The output capacitance is calculated as follows:

\[ C_{out} = \frac{V_{o} \times U}{R \times f_{sw} \times \Delta V_{o}} \]  

(15)

Where \( \Delta I_{L} \) is the current ripples and \( \Delta V_{o} \) is the voltage ripples.

4. THE MODIFIED SUPERTWISTING SLIDING MODE CONTROLLER DESIGN:

The super twisting sliding mode control is one of the robust techniques widely used for controlling systems. Its main advantage lies in its ability to overcome the chattering phenomenon that appears in traditional SMC and not need any data about the controlled system. In this study, a modified super twisting SMC (M-STSMC) is developed to further enhance the tracking of the maximum power point and reduce steady-state oscillations. The designed technique based on replacing the integral action with a fractional integrator.

The chosen sliding surface and the mathematical model of the strategy is presented below:

\[ S = \left( \frac{I_{pv}}{V_{pv}} + \frac{dI_{pv}}{dV_{pv}} \right) \]  

(16)

Therefore, to achieve the maximum power point, the surface must be forced to zero by the super twisting SMC. The control law contains two principal terms as follows:

\[ U = U_{eq} + U_{STSMC} \]  

(17)

The equivalent term is calculated using the following equation:

\[ \dot{S} = \left[ \frac{dS}{dX} \right]^{T} \dot{X} = 0 \]  

(18)

\[
\begin{align*}
\dot{X} &= f(X) + g(X) U_{eq} \\
X &= \left[ \begin{array}{c} I_{pv} \\
V_{o} \end{array} \right] f(X) = \frac{V_{pv} - V_{o}}{L} \\
g(X) = \frac{V_{o}}{C_{out}R} \left[ \begin{array}{c} I_{pv} \\
V_{o} \end{array} \right] \end{align*}
\]  

(19)

(20)

So, the equivalent control \( U_{eq} \) equals:
The second term is given in equation (22), [13]:
\[ U_{\text{STSMC}} = -\lambda |S| \text{sign}(S) - W \int \text{sign}(S) \] (22)
The sufficient conditions to ensure the finite convergence time are:
\[ W > \Phi \]
\[ \lambda^2 > \frac{4\Phi}{\Gamma_M (w + \Phi)} \]
\[ \frac{\Gamma^2_m}{\Gamma_m (w + \Phi)} \]
\[ 0 < \rho < 0.5 \] (23)

Where \( \Gamma_M, \Gamma_m, \Phi \) are positive constants and \( W, \lambda, \gamma, \rho \) are the control gains. Therefore, the control equation becomes:
\[ U = \left( 1 - \frac{V_{pv}}{V_o} \right) - \lambda |S| \text{sign}(S) - W \int \text{sign}(S) \] (24)

5. DISCUSSION AND RESULTS:
In this study, a modified STSMC is developed to achieve the maximum power point in photovoltaic system under different levels of irradiation. The strategy is designed also to optimize the performance of the conventional STSMC, enhance its efficiency, and minimize the chattering phenomenon occurred and effect about the power quality. The simulation is implemented in MATLAB/SIMULINK, and the results are presented as a comparison between the classical STSMC and the modified STSMC proposed in this study.
From Fig. 6, Fig. 7, Fig. 8, and Fig. 9, we can see the improvement in voltage and current results using the M-STSMC. The steady state oscillations are reduced compared to the STSMC method, so to get a required power quality to supply the charge efficiently.

1. CONCLUSION:
In order to track the maximum power point in PV systems and enhance their efficiency and performance, many nonlinear control methods have been developed and proposed. In this paper, a modified STSMC is designed to improve the conventional STSMC and obtains maximum power, while reducing the chattering phenomenon. The obtained results show an improvement in the performances under variations of irradiance by dint of the mediation of a fractional integrator in the traditional STSMC, which increases its flexibility.

References


