

# Squirrel Cage Induction Motor (SCIM) Rotor Flux Estimation and Observer Using Multivariable Sliding Mode Control (MSMC)

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**Abstract:** This paper proposes a multivariable sliding mode control (MSMC) based in rotor flux estimation and observer methods for squirrel cage induction motor (SCIM).

The principle of sliding mode control (SMC) adjustment can also be applied to multivariable systems. In this case, for each control quantity, there is a control member who switches the latter quickly between a maximum value and a minimum value, thus causing the sliding mode to appear. This article will discuss sliding mode tuning of multivariable systems, highlighting issues that arise in relation to mono-variable systems studied so far. In this paper, we will establish the general relationships, where we introduce the regulators of multivariable systems. To describe the behavior in sliding mode, we will call or equivalent control vector, at the end of this article we will introduce a rotor flux observer to improve the results obtained. The work is developed with a 2-level voltage source inverter. The simulation results are carried out to verify and validate the multivariable sliding mode control method proposed based rotor flux estimation and observer scheme

**Keywords:** SMC, MSMC, SCIM, Flux Estimation, Flux Observer

## 1. INTRODUCTION

The introduction section must contain theory related to the paper topic along with state of art study and well referenced citations. Make this section as informative as possible to justify the work and situate it with respect to the literature.

Direct current motors (DCM) have been widely used in areas requiring variable speed and position drives, due to the simplicity of controlling flux and torque from excitation current and armature current [1]. They operate - naturally - at maximum torque: the inductor field and the induced field are perpendicular thanks to the brush-collector system, which is not the case for other machines where the power engineer develops full ingenuity to obtain the same situation using power electronics and digital techniques [1], [2].

Currently, the use of alternating current motors, more particularly squirrel cage induction motors (SCIM), is more and more frequent, because these machines are characterized by their robustness and longevity, although these require structures internal and more complex control strategies. In order to obtain performances similar to those of the DCM with cage motors which can be based on wound rotor asynchronous

motors as well as on synchronous machines, it was necessary to separate the flow control and the control of the current generating the electromagnetic torque to introduce vector control (FOC) based on PI regulators [3], [4], [5].

Classic control techniques (PI regulators for example) require perfect knowledge of the model of the system to be adjusted. These approaches lead to control laws whose performance is strongly linked to the fidelity of the dynamic model used to describe the behavior of the system. Modeling errors or parametric variations of the system can deteriorate the performance of the adjustment since they contribute directly to the calculation of the control.

In order to solve such problems, the proposal of new control techniques is essential [5], [6], [7], [8].

Another type of modern controls that has attracted many researchers in recent years is sliding mode control. The recent interest in this control is mainly due to the availability of switches with high switching frequency and high-performance microprocessors [9], [10]. The sliding mode is a particular mode of operation of systems with variable structure [11]. In sliding mode tuning, the control switches between two different values following the sign of a switching function



$$\dot{S}_1(x) = \begin{pmatrix} \dot{\omega}_m + \frac{f}{J} \cdot \omega_m + \frac{P}{J} \cdot T_R \\ \dot{\phi}_{Rd} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rd} \\ \dot{\phi}_{Rq} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rq} \end{pmatrix} + \begin{pmatrix} \frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rq} & -\frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rd} & 0 \\ -\frac{R_R \cdot M}{L_R} & 0 & -\phi_{Rq} \\ 0 & -\frac{R_R \cdot M}{L_R} & \phi_{Rd} \end{pmatrix} \begin{pmatrix} I_{Sd} \\ I_{Sq} \\ \omega_R \end{pmatrix} \quad (12)$$

Replacing,  $I_{Sd}$ ,  $I_{Sq}$  and  $\omega_R$  by

$$I_{Sd}^* = I_{Sdeq} + I_{Sdn}, I_{Sq}^* = I_{Sqe} + I_{Sqn} \text{ and } \omega_R^* = \omega_{Re} + \omega_{Rn} \text{ we find :}$$

$$\dot{S}_1(x) = \begin{pmatrix} \dot{\omega}_m + \frac{f}{J} \cdot \omega_m + \frac{P}{J} \cdot T_R \\ \dot{\phi}_{Rd} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rd} \\ \dot{\phi}_{Rq} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rq} \end{pmatrix} + \begin{pmatrix} \frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rq} & -\frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rd} & 0 \\ -\frac{R_R \cdot M}{L_R} & 0 & -\phi_{Rq} \\ 0 & -\frac{R_R \cdot M}{L_R} & \phi_{Rd} \end{pmatrix} \times \begin{pmatrix} I_{Sdeq} + I_{Sdn} \\ I_{Sqe} + I_{Sqn} \\ \omega_{Re} + \omega_{Rn} \end{pmatrix} \quad (13)$$

$$\begin{pmatrix} I_{Sdeq} \\ I_{Sqe} \\ \omega_{Re} \end{pmatrix} = \begin{pmatrix} \frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rq} & -\frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rd} & 0 \\ -\frac{R_R \cdot M}{L_R} & 0 & -\phi_{Rq} \\ 0 & -\frac{R_R \cdot M}{L_R} & \phi_{Rd} \end{pmatrix}^{-1} \times \begin{pmatrix} \dot{\omega}_m + \frac{f}{J} \cdot \omega_m + \frac{P}{J} \cdot T_R \\ \dot{\phi}_{Rd} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rd} \\ \dot{\phi}_{Rq} + \frac{R_R \cdot M}{L_R} \cdot \phi_{Rq} \end{pmatrix} \quad (14)$$

$$\begin{pmatrix} I_{Sdn} \\ I_{Sqn} \\ \omega_{Rn} \end{pmatrix} = \begin{pmatrix} \frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rq} & -\frac{P^2 \cdot M}{J \cdot L_R} \cdot \phi_{Rd} & 0 \\ -\frac{R_R \cdot M}{L_R} & 0 & -\phi_{Rq} \\ 0 & -\frac{R_R \cdot M}{L_R} & \phi_{Rd} \end{pmatrix}^{-1} \times \begin{pmatrix} K_{fd} & 0 & 0 \\ 0 & K_{fq} & 0 \\ 0 & 0 & K_{\omega} \end{pmatrix} \cdot \text{Sign}(S_1(x)) \quad (15)$$

C. adjustment surface of the S2 system

$$S_2(x) = \begin{pmatrix} I_{Sd}^* - I_{Sd} \\ I_{Sq}^* - I_{Sq} \end{pmatrix} \quad (16)$$

The derivatives of the surfaces are:

$$\dot{S}_2(x) = \begin{pmatrix} \dot{I}_{Sd}^* - \dot{I}_{Sd} \\ \dot{I}_{Sq}^* - \dot{I}_{Sq} \end{pmatrix} \quad (17)$$

$$\dot{S}_2(x) = \begin{pmatrix} \dot{I}_{Sd}^* + \frac{1}{\sigma \cdot L_S} \cdot \left( R_S + \frac{R_R \cdot M^2}{L_R^2} \right) \cdot I_{Sd} - \omega_S \cdot I_{Sq} - \frac{R_R \cdot M}{\sigma \cdot L_S \cdot L_R^2} \cdot \phi_{Rd} - \frac{M \cdot \omega_m}{\sigma \cdot L_S \cdot L_R} \cdot \phi_{Rq} - \frac{1}{\sigma \cdot L_S} \cdot V_{Sd} \\ \dot{I}_{Sq}^* + \omega_S \cdot I_{Sd} + \frac{1}{\sigma \cdot L_S} \cdot \left( R_S + \frac{R_R \cdot M^2}{L_R^2} \right) \cdot I_{Sq} + \frac{M \cdot \omega_m}{\sigma \cdot L_S \cdot L_R} \cdot \phi_{Rd} - \frac{M \cdot R_R}{\sigma \cdot L_S \cdot L_R^2} \cdot \phi_{Rq} - \frac{1}{\sigma \cdot L_S} \cdot V_{Sq} \end{pmatrix} \quad (18)$$

Replacing,  $V_{Sd}$ ,  $V_{Sq}$  by  $V_{Sd}^* = V_{Sdeq} + V_{Sdn}$ ,

$$\dot{S}_2(x) = \begin{pmatrix} \dot{I}_{Sd}^* + \frac{1}{\sigma \cdot L_S} \cdot \left( R_S + \frac{R_R \cdot M^2}{L_R^2} \right) \cdot I_{Sd}^* - \omega_S \cdot I_{Sq}^* - \frac{M \cdot R_R}{\sigma \cdot L_S \cdot L_R^2} \cdot \phi_{Rd} - \frac{M \cdot \omega_m}{\sigma \cdot L_S \cdot L_R} \cdot \phi_{Rq} \\ \dot{I}_{Sq}^* + \omega_S \cdot I_{Sd}^* + \frac{1}{\sigma \cdot L_S} \cdot \left( R_S + \frac{R_R \cdot M^2}{L_R^2} \right) \cdot I_{Sq}^* + \frac{M \cdot \omega_m}{\sigma \cdot L_S \cdot L_R} \cdot \phi_{Rd} - \frac{M \cdot R_R}{\sigma \cdot L_S \cdot L_R^2} \cdot \phi_{Rq} \end{pmatrix} + \begin{pmatrix} -\frac{1}{\sigma \cdot L_S} & 0 \\ 0 & -\frac{1}{\sigma \cdot L_S} \end{pmatrix} \times \begin{pmatrix} V_{Sdeq} + V_{Sdn} \\ V_{Sqe} + V_{Sqn} \end{pmatrix} \quad (19)$$

$V_{S_q}^* = V_{S_{deq}} + V_{S_{qn}}$  we find

$$\begin{pmatrix} V_{S_{deq}} \\ V_{S_{qn}} \end{pmatrix} = \begin{pmatrix} -\frac{1}{\sigma.L_S} & 0 \\ 0 & -\frac{1}{\sigma.L_S} \end{pmatrix}^{-1} \times \begin{pmatrix} \dot{I}_{S_d}^* + \frac{1}{\sigma.L_S} \left( R_S + \frac{R_R.M^2}{L_R^2} \right) I_{S_d}^* - \omega_S.I_{S_q}^* - \\ -\frac{M.R_R}{\sigma.L_S.L_R^2} \hat{\phi}_{R_d} - \frac{M.\omega_m}{\sigma.L_S.L_R} \hat{\phi}_{R_q} \\ \dot{I}_{S_q}^* + \omega_S.I_{S_d}^* + \frac{1}{\sigma.L_S} \left( R_S + \frac{R_R.M^2}{L_R^2} \right) I_{S_q}^* + \\ + \frac{M.\omega_m}{\sigma.L_S.L_R} \hat{\phi}_{R_d} - \frac{M.R_R}{\sigma.L_S.L_R^2} \hat{\phi}_{R_q} \end{pmatrix} \quad (20)$$

$$\begin{pmatrix} V_{S_{dn}} \\ V_{S_{qn}} \end{pmatrix} = \begin{pmatrix} -\frac{1}{\sigma.L_S} & 0 \\ 0 & -\frac{1}{\sigma.L_S} \end{pmatrix}^{-1} \times \begin{pmatrix} K_d & 0 \\ 0 & K_q \end{pmatrix} \cdot \text{Sign}(S_2(x)) \quad (21)$$

D. Diagram of a multivariable sliding mode control with rotor flux estimation

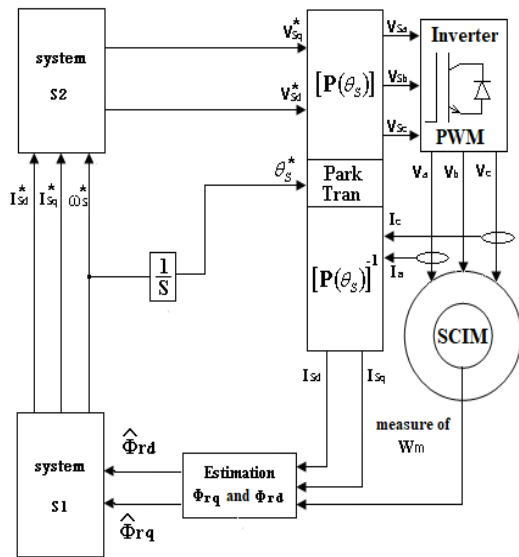


Fig. 1 Multivariable sliding mode control diagrams of Squirrel Cage Induction Motor (SCIM) (Flux estimation).

E. Simulation Results.

For verifying the proposed rotor flux observer of the SCIM, the simulations are carried out. SCIM is considered in the simulation and parameters as given in Appendix (Table 1). The multivariable sliding mode control (MSMC) has been implemented in MATLAB/SIMULINK.

The multivariable sliding mode control (MSMC) algorithm is compared using the same rotor speed reference command.

The simulation results are shown in Figs 2-7 (stator currents direct and quadrature, rotor flux direct and quadrature, Speed of SCIM and Electromagnetic torque of SCIM).

The SCIM runs in speed regulation at 150 rpm between  $t = 0$  until  $t = 2s$ , it undergoes a disturbance presented by the torque resisting at  $t = 1s$ , the speed reference will change by 150 rpm a - 150 rpm. The current  $I_{sq}$  perfectly follows its reference  $I_{sq}^*$  throughout the test. The current  $\Phi_{rd}$  remains constant and equal to its reference value ( $\Phi_r = 1$  w). The flux  $\Phi_{rq}$  is simulated all the time, which proves the effectiveness of the control based on the rotor flux estimator.

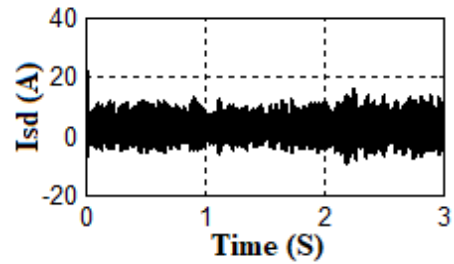


Fig. 2 Stator current direct.

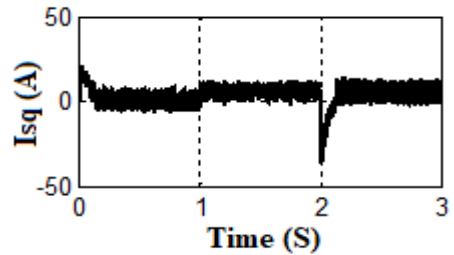


Fig. 3 Stator current quadrature.

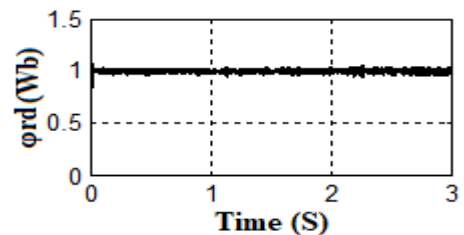


Fig. 4 Rotor flux direct.

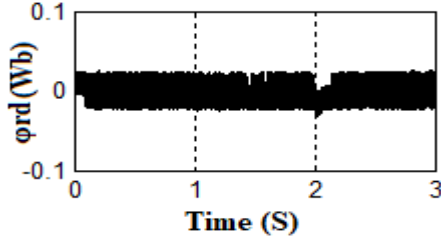


Fig. 5 Rotor flux quadrature.

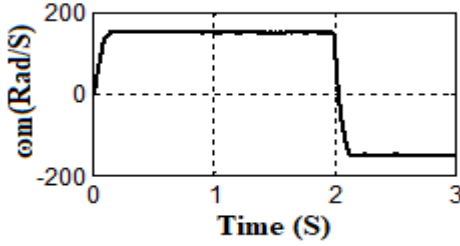


Fig. 6 Speed of SCIM.

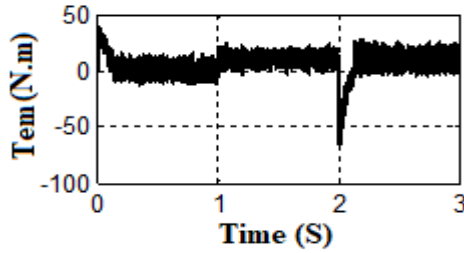


Fig. 7 Electromagnetic torque.

#### 4. MULTIVARIABLE SLIDING MODE CONTROL WITH ROTOR FLUX OBSERVER

We have the following equations of state for the stator voltages:

$$\begin{cases} V_{sd} = R_s \cdot I_{sd} + \sigma L_s \cdot \frac{dI_{sd}}{dt} + \frac{M}{L_R} \frac{d\phi_{rd}}{dt} - \\ - \omega_s \sigma L_s \cdot I_{sq} - \omega_s \frac{M}{L_R} \cdot \phi_{rq} \end{cases} \quad (22)$$

$$\begin{cases} V_{sq} = R_s \cdot I_{sq} + \sigma L_s \cdot \frac{dI_{sq}}{dt} + \\ + \frac{M}{L_R} \frac{d\phi_{rq}}{dt} - \omega_s \sigma L_s \cdot I_{sd} - \omega_s \frac{M}{L_R} \cdot \phi_{rd} \end{cases}$$

$$\begin{cases} V_s = \begin{bmatrix} V_{sd} \\ V_{sq} \end{bmatrix} = R_s \cdot I_s + \sigma L_s \cdot \dot{I}_s + \frac{M}{L_R} \cdot I_s \cdot \dot{\phi}_R + \\ + \omega_s \cdot \sigma L_s \cdot J \cdot I_s + \omega_s \cdot \frac{M}{L_R} \cdot J \cdot \phi_R \end{cases} \quad (23)$$

$$\begin{cases} \hat{V}_s = \begin{bmatrix} \hat{V}_{sd} \\ \hat{V}_{sq} \end{bmatrix} = R_s \cdot I_s + \sigma L_s \cdot \dot{I}_s + \frac{M}{L_R} \cdot I_s \cdot \dot{\hat{\phi}}_R + \\ + \omega_s \cdot \sigma L_s \cdot J \cdot I_s + \omega_s \cdot \frac{M}{L_R} \cdot J \cdot \hat{\phi}_R \end{cases}$$

$$\begin{cases} \frac{d\hat{\phi}_{rd}}{dt} = \dot{\hat{\phi}}_{rd} = -\frac{\phi_{rd}}{T_R} + \omega_g \cdot \phi_{rq} + \frac{M}{T_R} \cdot I_{sd} \end{cases} \quad (24)$$

$$\begin{cases} \frac{d\hat{\phi}_{rq}}{dt} = \dot{\hat{\phi}}_{rq} = -\frac{\phi_{rq}}{T_R} + \omega_g \cdot \phi_{rd} + \frac{M}{T_R} \cdot I_{sq} \end{cases}$$

Writing equations in matrix form:

$$\dot{\hat{\phi}} = \begin{bmatrix} -\frac{I}{T_R} - \omega_g \cdot J \\ \frac{M}{T_R} \cdot I \cdot I_s + K \cdot (\hat{V}_s - V_s) \end{bmatrix} \cdot \hat{\phi}_R \quad (25)$$

With  $K = k \cdot I = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$ .

k : is the observer's gain.

Observer error:  $e = \hat{\phi}_R - \phi_R$  (26)

The derivative of the error is:

$$\dot{e} = \dot{\hat{\phi}} - \dot{\phi} = \begin{bmatrix} -\frac{I}{T_R} + J \left( \omega_g - K \cdot \omega_s \cdot \frac{M}{L_R} \right) \\ e + K \cdot \frac{M}{L_R} \cdot \dot{e} \end{bmatrix} \cdot e + K \cdot \frac{M}{L_R} \cdot \dot{e} \quad (27)$$

Let's put:  $\omega_0 = \omega_g - K \cdot \omega_s \cdot \frac{M}{L_R}$  (28)

From where:

$$\dot{e} = \left( I - \frac{K \cdot M}{L_R} \right)^{-1} \cdot \left( -\frac{I}{T_R} - J \cdot \omega_0 \right) \cdot e \quad (29)$$

We now consider how to avoid having to bring derivatives into effect. First define the fallback variable:

$$z = [I - K \cdot (M/L_R)] \cdot \hat{\phi}_R - K \cdot (\sigma L_s) \cdot I_s \quad (30)$$

$$\dot{z} = [I - K \cdot (M/L_R)] \cdot \dot{\hat{\phi}} - K \cdot (\sigma L_s) \cdot \dot{I}_s \quad (31)$$

From the equation (31) we draw:

$$\begin{aligned} \sigma L_s \cdot \dot{I}_s &= \hat{V}_s - (R_s \cdot I_s + \omega_s \cdot \sigma L_s \cdot J) \cdot I_s - \\ - \frac{M}{L_R} \cdot I_s \cdot \dot{\hat{\phi}}_R - \omega_s \cdot \frac{M}{L_R} \cdot J \cdot \hat{\phi}_R \end{aligned} \quad (32)$$

Using the equation (32) in the equation (31) we obtain:

$$\begin{aligned} \dot{z} &= \dot{\hat{\phi}}_R + K \cdot (R_s \cdot I_s + \omega_s \cdot \sigma L_s \cdot J) \cdot I_s + \\ + K \cdot \omega_s \cdot \frac{M}{L_R} \cdot J \cdot \hat{\phi}_R - K \cdot \hat{V}_s \end{aligned} \quad (33)$$

Substitute  $\dot{\hat{\phi}}_R$  by its value in the equation (33) we find:

$$\begin{aligned} \dot{z} &= \dot{\hat{\phi}}_R + K \cdot (R_s \cdot I_s + \omega_s \cdot \sigma L_s \cdot J) \cdot I_s + \\ + K \cdot \omega_s \cdot \frac{M}{L_R} \cdot J \cdot \hat{\phi}_R - K \cdot \hat{V}_s \end{aligned} \quad (34)$$

Now show that:

$$\hat{\phi}_R = \left( I - K \cdot \frac{M}{L_R} \right)^{-1} \cdot (z + K \cdot \sigma L_s \cdot I_s) \quad (35)$$

A. Diagram of a multivariable sliding mode control with rotor flux observer

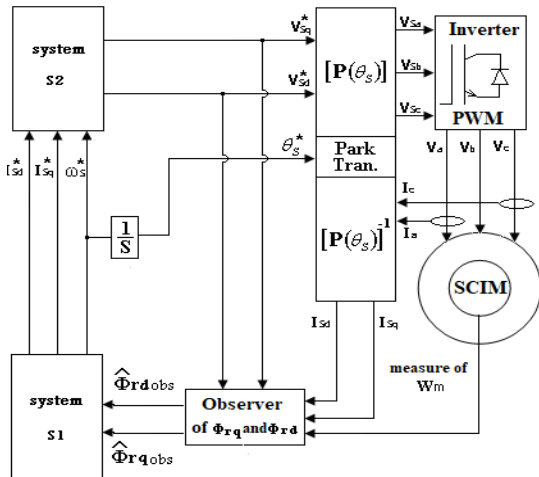


Fig. 8 Multivariable sliding mode control diagrams of Squirrel Cage Induction Motor (SCIM) (Flux observer).

B. Simulation Results

For verifying the proposed rotor flux estimation of the SCIM, the simulations are carried out. SCIM is considered in the simulation and parameters as given in Appendix (Table 1).

The multivariable sliding mode controller (MSMC) algorithm is compared using the same rotor speed reference command.

The simulation results are shown in Figs 9-14 (stator currents direct and quadrature, rotor flux direct and quadrature, Speed of SCIM and Electromagnetic torque of SCIM).

The SCIM runs in speed regulation at 150 rpm between  $t = 0$  until  $t = 2s$ , it undergoes a disturbance presented by the torque resisting at  $t = 1s$ , the speed reference will change by 150 rpm a - 150 rpm. The current  $I_{sq}$  perfectly follows its reference  $I_{sq}^*$  throughout the test. The current  $\Phi_{rd}$  remains constant and equal to its reference value ( $\Phi_r = 1$  Wb). The flux  $\Phi_{rq}$  is simulated all the time, which proves the effectiveness of the control based on the rotor flux observer with the minimization and elimination of disturbances on the different electrical quantities.

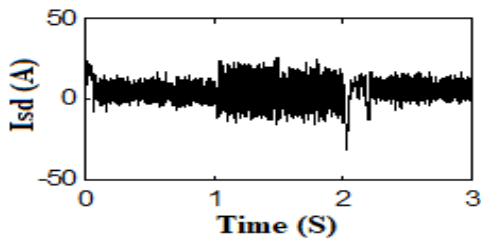


Fig. 9 Stator current direct.

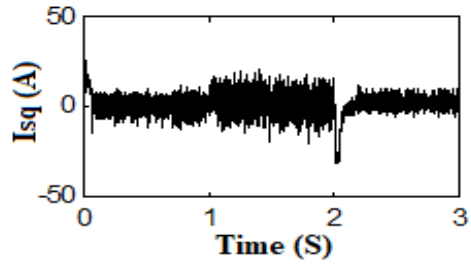


Fig. 10 Stator current quadrature.

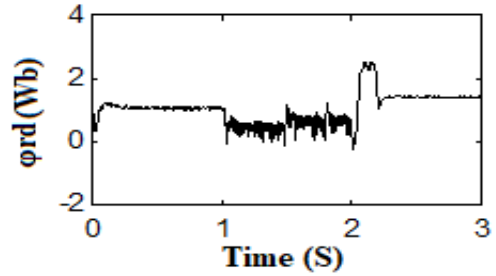


Fig. 11 Rotor flux direct.

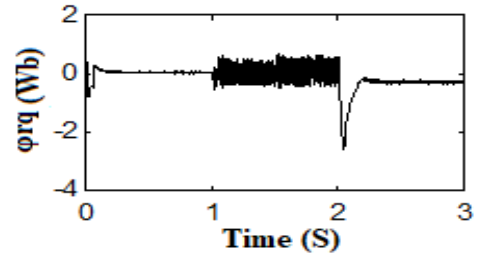


Fig. 12 Rotor flux quadrature.

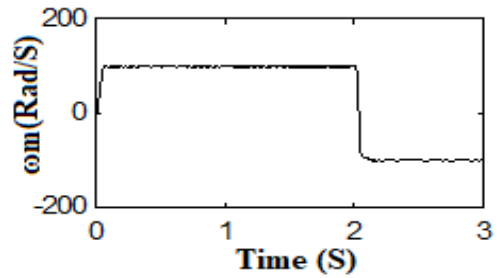


Fig. 13 Speed of SCIM.

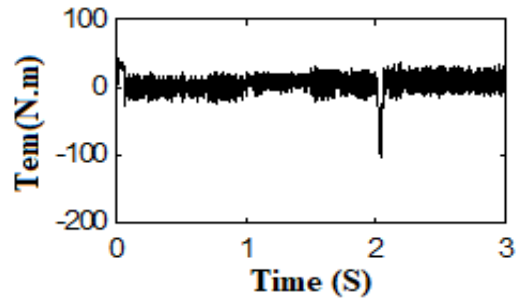


Fig. 14 Electromagnetic torque.



**5. CONCLUSION**

This paper has proposed a multivariable sliding mode control (MSMC) for based estimation and observer method for the rotor flux of squirrel cage induction motor (SCIM). With the use of multivariable sliding mode control (MSMC), using a rotor flux estimator, more improved results were obtained than other methods of controls seen previously either at the disturbance level or at the set point tracking level, but with the implementation of an observer by sliding mode, thanks to which it is possible to collect information on the rotor flux, the simulation results have showed the effectiveness of such an observer, as well as its robustness properties by taking into account variations in mechanical speed.

**6. APPENDIX**

Table 1 The parameters of the SCIM

| Parameters                       | Values                  |
|----------------------------------|-------------------------|
| Rated power                      | 1.5 kW                  |
| Line voltage                     | 230 V                   |
| Line current                     | 3.64A/6.31A             |
| Stator resistance $R_s$          | 4.85 $\Omega$           |
| Rotor resistance $R_r$           | 3.805 $\Omega$          |
| Stator inductance $L_s$          | 0.274 H                 |
| Rotor inductance $L_r$           | 0.274 H                 |
| Magnetising inductance $M$       | 0.258 H                 |
| Moment of inertia $J$            | 0.031 Kg.m <sup>2</sup> |
| Viscous friction coefficient $f$ | 0.008 N.s/rd            |
| Number of pole pairs             | 2                       |

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